

**Instructions:** Show all work. Use exact answers unless specifically asked to round. Be sure to complete all parts of each question.

1. Find the critical points of the function  $f(x, y) = x^2 - 3xy + 2y^2 + 4y$  and characterize each as a maximum, minimum or saddle point.
2. Find the absolute extrema for the function  $f(x, y) = x^2 - 2y^2$  on the region bounded by  $y = 4 - x^2$  and  $y = -5$ .
3. Find an appropriate change of variables for the region bounded by the sides of the rectangle with vertices  $(0,0)$ ,  $(3,4)$ ,  $(0,8)$ , and  $(-3,4)$ . Calculate the value of the Jacobian, and use that information to find the value of the integral  $\int_A \int (3x + 4y)^2 e^{4x+3y} dA$  over the indicated rectangle.