

**Instructions:** Show all work. Justify answers as completely as possible. If you are asked to prove something, mere computation is not enough. You must explain your reasoning. Be sure to state your conclusion clearly. Incomplete work or justification will not receive full credit. Use exact answers unless specifically asked to round.

1. Prove the identity  $x + yz = (x + y)(x + z)$  using Boolean functions.

$x$	$y$	$z$	$yz$	$x + yz$	$x + y$	$x + z$	$(x + y)(x + z)$
1	1	1	1	1	1	1	1
1	1	0	0	1	1	1	1
1	0	1	0	1	1	1	1
1	0	0	0	1	1	1	1
0	1	1	1	1	1	1	1
0	1	0	0	0	1	0	0
0	0	1	0	0	0	1	0
0	0	0	0	0	0	0	0

↑  
The same

2. Find the dual  $F^d$  of the function  $F(x, y, z) = x\bar{y} + \overline{(xyz)}$ .

$$(x + \bar{y})(x + y + z)$$

3. Find the sum-of-products expansion of the Boolean function  $F(x, y, z) = (\bar{x} + y)z$ .

$$\begin{aligned} & \bar{x}z + yz \\ & (y + \bar{y})\bar{x}z + (x + \bar{x})yz \\ & \bar{x}yz + \bar{x}\bar{y}z + xyz + \bar{x}yz \\ & \bar{x}yz + \bar{x}\bar{y}z + xyz \end{aligned}$$