

Instructions: Show all work. Answers without work can only be graded all or nothing. Partial credit is available only when work is shown. Answer all parts of each problem. Provide explanations as indicated. You may use Excel to complete any required statistical calculations or graphs. Submit any Excel work with assignment. Do not say "see Excel" for answers, but write or paste them into this document. Exact answers are preferred unless specifically asked to round.

1. A dataset has 157 observations and the value 46 corresponds to the 112th observation.
- a. Estimate the percentile represented by the value 46.

$$112/157 = 0.7133... \quad \text{approx } 71^{\text{st}} \text{ percentile}$$

- b. At what position (rank) would one find the value corresponding to the 90th percentile?

$$0.90 \times 157 = 141.3 \quad \text{approx. the } 141^{\text{st}} \text{ position in the sorted list.}$$

2. Answer the questions that follow based on the contingency table shown, assuming that a random person is selected from the sample.

	Column Labels (Product Purchase Category)			
Row Labels (Homeownership)	Drink	Food	Non-Consumable	Grand Total
N	504	4023	1088	5615
Y	746	6130	1568	8444
Grand Total	1250	10153	2656	14059

- a. What is the probability that the person selected bought a food product?

$$10153/14059$$

- b. What is the probability that the person selected owns their own home?

$$8444/14059$$

- c. What is the probability that the person selected both owns their home and purchased food?

$$6130/14059$$

- d. What is the probability that the person selected either owns their own home or purchased food?

$$\frac{10153 + 8444 - 6130}{14059} = 12467/14059$$

- e. What is the probability that the person selected owns their home given that they purchased food?

$$6130/10153$$

- f. What is the probability that the person selected purchased food given that they owned their own home?

$$6130/8444$$

g. Is home ownership and food purchase independent? Explain (with math!).

it is not

$$P(\text{food}) = 10153/104059 \quad P(\text{food} | Y) = 6130/8444 \quad \text{which are not equal.}$$

3. Find the missing value in the discrete probability distribution shown below. Then find the mean of the distribution.

x	1	3	4	6	10
$p(x)$	0.15	0.21	0.06	0.28	? \leftarrow 0.30

4. A coin is flipped 15 times. In how many different ways can one obtain 6 heads? What is the probability of such a result?

$$\text{Count } \binom{15}{6} = {}^{15}C_6 = 5005$$

$$\text{prob. is binomial } \binom{15}{6} (0.5)^6 (0.5)^9 = \frac{5005}{2^{15}} = 0.15274$$