

Instructions: Show all work. Use exact answers unless specifically asked to round. Answer all parts of each question.

1. Solve each equation for x .

a. $e^{4x} + 5e^{2x} - 24 = 0$

$$u^2 + 5u - 24 = 0$$

$$(u+8)(u-3) = 0$$

$$u = -8, u = 3$$

$$u = e^{2x}$$

$$e^{2x} = -8 \quad \text{no solution}$$

$$e^{2x} = 3$$

$$2x = \ln 3$$

$$\boxed{x = \frac{1}{2} \ln 3}$$

- b. $\log x + \log(x+3) = \log 10$

$$\log(x(x+3)) = \log 10$$

$$x^2 + 3x - 10 = 0$$

$$(x+5)(x-2) = 0$$

$$x = -5, x = 2$$

$\log(-5)$ not defined

$$\boxed{x = 2}$$

2. Use Newton's Law of Cooling $T = C + (T_0 - c)e^{kt}$ to solve: a pizza removed from the oven has a temperature of 450°F . It is left sitting in a room that has a temperature of 70°F . After five minutes the pizza is 300°F . Find a model for the temperature of the cooling pizza and use that to find the temperature of the pizza after 20 minutes.

$$450 = T = 70 + (450 - c)e^{kt}$$

$$T = 70 + 380e^{kt}$$

$$300 = 70 + 380e^{5k}$$

$$230 = 380e^{5k}$$

$$\frac{230}{380} = e^{5k}$$

$$\ln\left(\frac{230}{380}\right) = 5k$$

$$k = -0.100418\dots$$

$$T = 70 + 380e^{-0.1004t}$$

$$T(20) = 70 + 380e^{-0.1004(20)}$$

$$= 120.99887\dots$$

$$\approx 121^\circ$$