

Instructions: Show all work. Use exact answers unless otherwise asked to round.

1. Determine the convergence or divergence of the sequence.

a. $a_n = \frac{\ln n^3}{2n}$

$$\lim_{n \rightarrow \infty} \frac{\ln(n^3)}{2n} = \lim_{n \rightarrow \infty} \frac{3 \ln n}{2n} = \lim_{n \rightarrow \infty} \frac{3 \cdot \frac{1}{n}}{2} = 0$$

b. $a_n = ne^{-n/2}$

$$\lim_{n \rightarrow \infty} ne^{-n/2} = \lim_{n \rightarrow \infty} \frac{n}{e^{n/2}} = \lim_{n \rightarrow \infty} \frac{1}{2e^{n/2}} = 0$$

2. Find the sum of the convergent geometric series $\sum_{n=0}^{\infty} \left(-\frac{1}{5}\right)^n$.

$$r = -\frac{1}{5}$$

$$S = \frac{1}{1 - (-1/5)} = \frac{1}{6/5} = \frac{5}{6}$$

3. Write $\sum_{n=1}^{\infty} \ln \frac{n+1}{n}$ as a telescoping series, then determine if the series converges or diverges.

$$\sum_{n=1}^{\infty} \ln(n+1) - \ln(n)$$

diverges

$$= \lim_{n \rightarrow \infty} \ln(n+1) - \ln(1) = \infty$$