

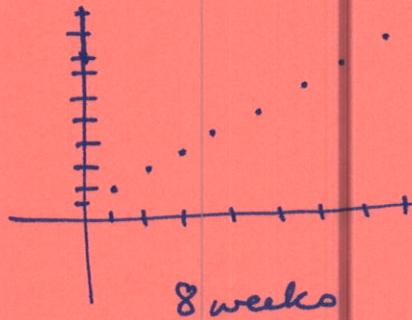
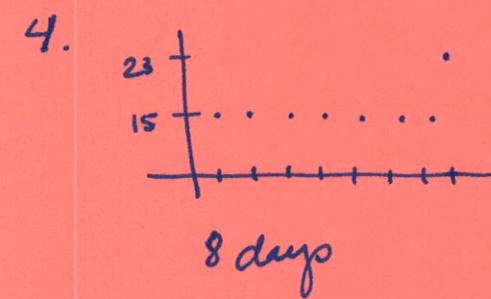
## MAT100 Homework #3 Key

1.  $A_n = d(n-1) + A_1$   
 ↑                   ↑  
 common difference   first term (if starting at  $A_1$ )

2.  $A_n = A_{n-1} + d$   
 ↑                   common difference  
 previous term

3.  $A_1 = 15 \quad d = 8$

$$A_{52} = 8(52-1) + 15 = 423$$



5.

$$\begin{array}{r} 5n = 8(n-1) + 15 \\ -15 \qquad \qquad \qquad -15 \\ \hline \frac{496}{8} = \frac{8(n-1)}{8} \\ 62 = n-1 \\ +1 \qquad +1 \\ \hline 63 = n \end{array}$$

63 weeks

6.  $A_1 = 2$

$$\begin{array}{r} 198 = 2(n-1) + 2 \\ -2 \qquad \qquad \qquad -2 \\ \hline \frac{196}{2} = \frac{2(n-1)}{2} \\ 98 = n-1 \\ +1 \qquad +1 \\ \hline 99 = n \end{array}$$

$$\begin{aligned} \text{Sum} &= \frac{(2+198)99}{2} \\ &= \frac{200}{2} \cdot 99 = 100 \cdot 99 \\ &= 9900 \end{aligned}$$

7. exponential

8.  $100 \left(1 + \frac{10}{12}\right)^6 = 105.11$

$$9. \text{ Sum} = \frac{100(1+1.01^n)}{1-1.01} = 1156.68\dots$$

$$10. A_1 = 10 \quad d = 1$$

$$A_{30} = 10 + \frac{(n-1)}{30} = 10 + 29 = 39 \quad \text{seats in final row}$$

$$\frac{(10+39)30}{2} = 735 \quad \text{seats in the section}$$

$$11. R = 1.02 \quad A_1 = 1,576,300 \quad \text{in 2015}$$

$$A_6 = \quad \text{in 2020}$$

$$A_N = 1,576,300 (1.02)^5 = 1,740,362$$

$$\frac{2 \times 1,576,300}{1,576,300} = (1.02)^{n-1} \quad \frac{(1,576,300)}{1,576,300} \quad n = 36.002789$$

$$2 = (1.02)^{n-1} \quad \boxed{\phantom{000}} \quad \text{in 2051}$$