Instructions: Show all work to receive full credit. You should note any formulas used or calculator functions used, their inputs and outputs. I cannot grade work if I don't know where an answer came from. Be sure complete all parts of each questions, including requests for interpretation and explanations. Be as thorough as possible.

1. The 100 tiles in Scrabble are distributed as follows:

| Tile | Number | Tile | Number | Tile | Number | 711 | T |
|-------|--------|------|--------|------|--------|------|--------|
| Blank | 2 | Α | 0 | | | Tile | Number |
| D | _ | | 9 | В | 2 | С | 2 |
| | 4 | E | 12 | F | 2 | G | 2 |
| Н | 2 | I | 9 | 1 | 1 | | 3 |
| L | 4 | M | 2 | N | | N C | 1 |
| Р | 2 | 0 | 1 | | 6 | 0 | 8 |
| - | 2 | ų | 1 | R | 6 | S | Δ |
| 1 | 6 | U | 4 | V | 2 | W | 1 |
| Х | 1 | Υ | 2 | Z | 1 | VV | 2 |

a. What is the probability of selecting an M as the first tile in a game? (5 points)

$$\frac{2}{100} = \frac{1}{50} = 2\%$$

b. What is the probability of selecting a S, T or D as the first tile? (6 points)

c. What is the probability of not selecting a blank? (5 points)

$$1 - \frac{2}{100} = \frac{98}{100} = 98\%$$

 d. What is the probability of selecting the word CAR in order from the first three tiles in a game? (7 points)

$$\frac{2}{100} \cdot \frac{9}{99} \cdot \frac{6}{98} = 1.11 \times 10^{-4}$$

e. Is the selection of letters in Scrabble independent? Why or why not? (4 points)

No. Since ofter selecting a tile There are fewer b choose from 3 the probability Changes

- 2. Determine the number of outcomes in each of the following scenarios. (7 points each)
 - a. A local area network requires eight characters for a username and is case sensitive, and the character can use numbers in the last two digits. How many usernames of this type are there?

$$52^6.62^2 = 7.5998 \times 10^{13}$$

b. Suppose that a lottery has 46 balls, and someone needs 7 matches in any order to win the top prize. How many possible winning number combinations are possible?

c. Suppose that nine horses are in a particular race. How many ways can the top three horses finish?

d. Tim is planning to create a word scramble puzzle out of the word RUMPELSTILTSKIN. How many different sequences of the letters are possible?

3. A charity sells 450 tickets for a raffle, costing \$10 per ticket. The top prize is \$500, a second prize of \$100, and two third prizes of \$50. For someone purchasing a ticket, what is the expected value? Interpret the value in the context of the problem. (10 points)

| Value | 490 | 90 | 40 | - 10 |
|-------------|-------|-------|-------|---------|
| Probability | 1/450 | 1/450 | 2/450 | 446/450 |

- 4. Four-fifths of drivers put their seat belt on when they get into a driving simulator. Use that fact to answer the following questions. (6 points each)
 - a. If 20 people get into the simulator, what is the probability that exactly 8 of the people will put on their seat belts?

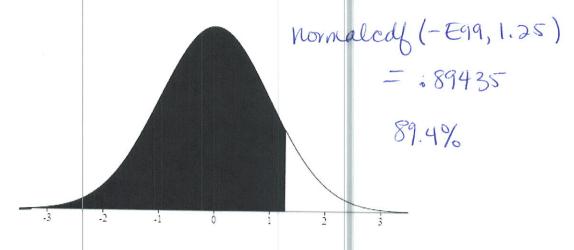
binomialpdf (20, 4/5, 8) = 8.657 × 10-5

b. If 20 people get into the simulator, what is the probability that at least than 15 people will put on their seat belts?

1- benomialed (20,4/5,14) = .8042

80.4%

- 5. Find the probability under the curve of the given normal distributions. (6 points each)
 - a. Standard normal distribution. Z-score at the boundary is 1.25.



- 6. The SAT has a mean score of 1498 and a standard deviation of 199. (5 points each)
 - a. What is the z-score of 1840?

b. What score represents the 80th percentile of the distribution? Round your answer to the nearest 10 points.

inv Norm (.80, 1498, 199) = 1665.48

c. If a school wants to admit only students with the top 10% of SAT scorers, what cut-off score is needed? Round your answer to the nearest 10 points.

d. The mean score on the ACT is 21 with a standard deviation of 5.2. Which student scored higher: Abby with a score of 31 on the ACT, or Barbara with a score of 2130 on the SAT?

$$Z_A = \frac{31-21}{5.2} = 1.923$$

higher score

- 7. For each of the following variables, determine i) is the variable qualitative or quantitative? ii) the level of measurement: nominal, ordinal, interval, or ratio? iii) if the variable is quantitative, is it discrete or continuous? (4 points each)
 - a. Date of birth

quantitative, discrete interval

b. Credit card brand

qualitative, nomenal

c. Social security number

qualitative, nonixal

d. Body weight

quantitatur, Continuous, vatio

8. A particular church choir was asked their ages. The results are shown below in a stemplot below. Key: 3|1 = 31.

Stemplot of ages in church choir

For the data above, find the following statistics:

a. The mean, median and mode (6 points)

$$\bar{X} = 26.87 \implies 26.9$$

 $\hat{X} = 26$

b. The standard deviation and range (6 points)

$$S_x = 9.10$$

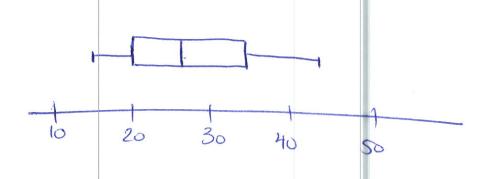
range = 43-15 = 28

c. Calculate the five-number summary for this data. (5 points)

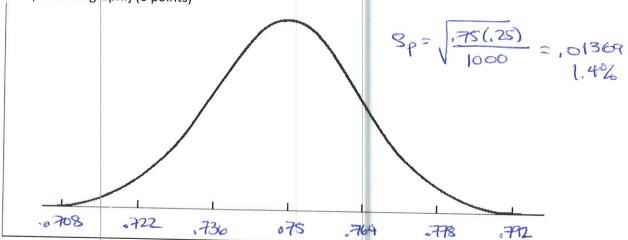
d. Use that information to construct a simple box plot. Be sure your graph is to scale. (7 points)

no mode: 15, 23, 26, 43

all repeated turce



9. If the population proportion is p=0.75. Sketch the sampling distribution on the normal curve below for sample of 1000 people. [Hint: You will need to calculate the standard error to complete the graph.] (6 points)

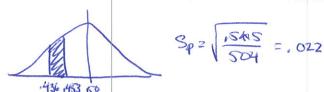


10. A recent poll placed a head-to-head match-up between Hillary Clinton and Donald Trump at 48% Clinton, 41% Trump based on a national poll of 504 people. Construct the 95% confidence interval around both the Clinton and Trump values.

- a. Clinton: (,43654, ,52378)
- b. Trump: (.36776, .45366)

- (8 points)
- c. Do the two confidence intervals overlap? If so, in what range of values? (5 points)

d. If we assume conservatively that the true population proportion is close to 50%, what is the probability that Clinton and Trump are actually tied or their positions are reversed? [Hint: find the probability that the values are normally distributed with a mean of 50%, and falls between the two values in part c. If there is no overlap, report "less than 5%".] (4 points)



normalcolf (.43654, .45366, .50, .022) = .0156 The area of world is so small that they are almost certainly not trid or switched places 11. A Gallup poll taken in 1978 asked 1006 Americans how many books they read in the past year. They found a mean of 18.8 with a standard deviation of 19.8 books. [Note: This results suggests the distribution is very skewed.] Calculate a 99% confidence interval for these results. (points)

T-Inkwal (Stats) x = 18.8

use t-dishibution since the results one very showed

n=1006

Sx = 19.8

C-level: 99

(17,189,20.411)

12. Complete the table below. Two of the boxes are labeled "Correct Decision"; label the other two boxes Type I Error or Type II Error as appropriate. (8 points)

| | H _o True | H _o False |
|----------------------|---------------------|----------------------|
| Reject Ho | TypeI | Correct Decision |
| Fail to Reject Ho | Connect Decesión | Type II Error |

13. In a survey conducted by the American Animal Hospital Association, 37% of respondents stated that they talk to their pets on the answering machine or telephone. A vet found this hard to believe so he questioned 150 pet owners and discovered that 54 of them spoke to their pets on the answering machine or telephone. Does the vet have sufficient evidence to maintain his skepticism? (8 points)

1 PropZTest

Ho: p = .37Ha: $p \neq .37$

There is not sufficient lordence for The ver to maintain his shephiism

Po= ,37 X = 54

N=150

Prop # Po

P= ,7997 fail to reject to

14. In 1990, the mean height of women 20 years of age or older was 63.7 inches based on data from the CDC, with a standard deviation of 3.4 inches. Suppose that a random sample of 45 women who are 20 years old or older today produced a mean of 63.9 inches. Is this strong evidence that women are taller now than 25 years ago? (10 points)

to: u=63.7 Ha: 4>63.7

Ztest (Stats)

 $M_0 = 63.7$ N = 45 $\sigma = 3.4$ $M > \mu_0$ X = 63.9

7= 3946

P= ,346569 >.05

fail to reject the This is not sufficient evidence to Think armen are taller today

15. A random sample of 1201 Americans, it was discovered that 1139 of them lived in neighborhoods with acceptable levels of carbon monoxide. You'd like to construct a 99% confidence interval for this measurement with a margin of error of only 0.5%. What sample size is needed to achieve this result? (10 points)

 $N = \rho (\Gamma \rho) \left(\frac{2\sigma_{12}}{F} \right)^{2}$

 $N = \frac{1139}{1201} \cdot \frac{63}{1201} \left(\frac{2.5758}{005} \right)^3 = 12.993.12653$

à Sample site & at least 12,994
people is required