

Instructions: Show all work for full credit.

1. Consider the weighted voting system [28: 21, 18, 12, 3].  
 a. Calculate the Banzhaf power distribution for this system.

- $\{P_1, P_2, P_3, P_4\}$
- $\{P_1, P_2, P_3\}$
- $\{P_1, P_2, P_4\}$
- $\{P_1, P_3, P_4\}$
- $\{P_2, P_3, P_4\}$
- $\{P_1, P_2\}$
- $\{P_1, P_3\}$
- $\{P_2, P_3\}$

critical players 12

$$P_1: \frac{4}{12} = 33\%$$

$$P_2: \frac{4}{12} = 33\%$$

$$P_3 = \frac{4}{12} = 33\%$$

$$P_4 = \frac{0}{12} = 0\%$$

dummy  
no veto power

- b. Calculate the Shapley-Shubik power distribution for this system.

- |                                      |                                      |
|--------------------------------------|--------------------------------------|
| $\langle P_1, P_2, P_3, P_4 \rangle$ | $\langle P_3, P_1, P_2, P_4 \rangle$ |
| $\langle P_1, P_2, P_4, P_3 \rangle$ | $\langle P_3, P_1, P_4, P_2 \rangle$ |
| $\langle P_1, P_3, P_2, P_4 \rangle$ | $\langle P_3, P_2, P_1, P_4 \rangle$ |
| $\langle P_1, P_3, P_4, P_2 \rangle$ | $\langle P_3, P_2, P_4, P_1 \rangle$ |
| $\langle P_1, P_4, P_2, P_3 \rangle$ | $\langle P_3, P_4, P_2, P_1 \rangle$ |
| $\langle P_1, P_4, P_3, P_2 \rangle$ | $\langle P_3, P_4, P_1, P_2 \rangle$ |
| $\langle P_2, P_1, P_3, P_4 \rangle$ | $\langle P_4, P_1, P_2, P_3 \rangle$ |
| $\langle P_2, P_1, P_4, P_3 \rangle$ | $\langle P_4, P_1, P_3, P_2 \rangle$ |
| $\langle P_2, P_3, P_1, P_4 \rangle$ | $\langle P_4, P_2, P_1, P_3 \rangle$ |
| $\langle P_2, P_3, P_4, P_1 \rangle$ | $\langle P_4, P_2, P_3, P_1 \rangle$ |
| $\langle P_2, P_4, P_1, P_3 \rangle$ | $\langle P_4, P_3, P_1, P_2 \rangle$ |
| $\langle P_2, P_4, P_3, P_1 \rangle$ | $\langle P_4, P_3, P_2, P_1 \rangle$ |

$$P_1: \frac{8}{24} = 33\%$$

$$P_2: \frac{8}{24} = 33\%$$

$$P_3: \frac{8}{24} = 33\%$$

$$P_4 = \frac{0}{24} = 0\%$$