

Introduction to Multivariable Functions

Learning Objectives

- Evaluate a multivariable function
 - Sketch a point in three-dimensional space
 - Graph a cross section of a multivariable function
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Evaluate a multivariable function

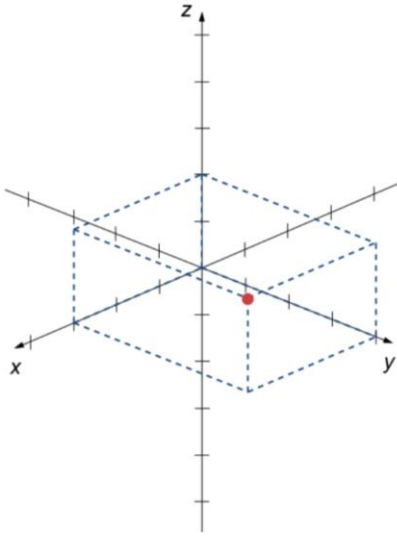
1. Evaluate each multivariable function at the indicated point.

a. $f(x, y) = x^2 + 2xy - 4y^2, (1, -2)$

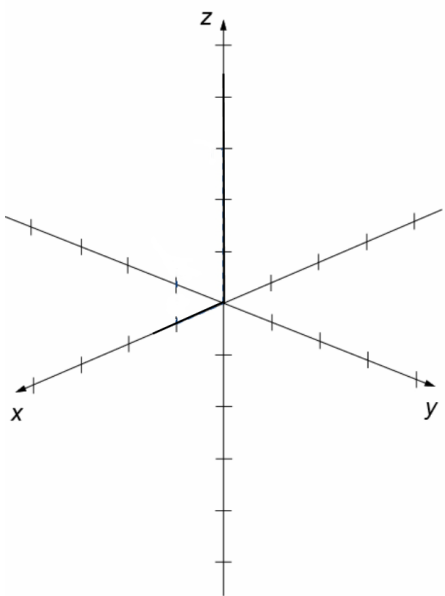
b. $f(x, y, z) = z^2 e^{xy} - \frac{z}{1+x^2 y^2}, (4, 0, -2)$

Sketch a point in three-dimensional space

2. Identify the point shown in the graph.



3. Plot the point $(4, 1, -1)$ on the graph below.



Graph cross sections of a multivariable function

4. Sketch the cross-section of the graph $f(x, y) = x^2 + 2xy - 4y^2$ for each condition.

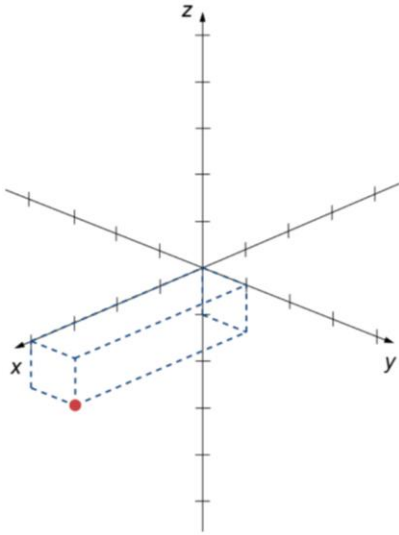
a. $x = 1$

b. $y = -1$

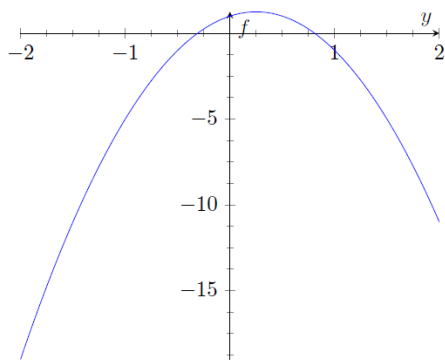
ANSWER KEY

1. a. -19; b. 6

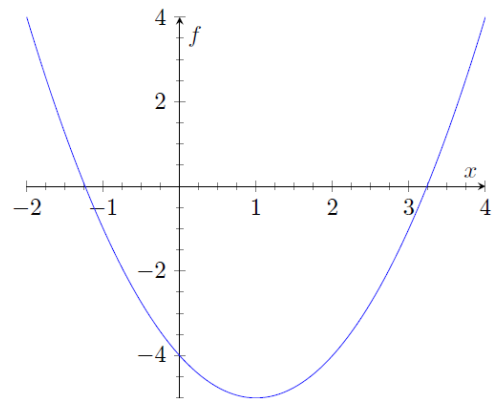
2. (3,4,2)



3.



4. a.



b.