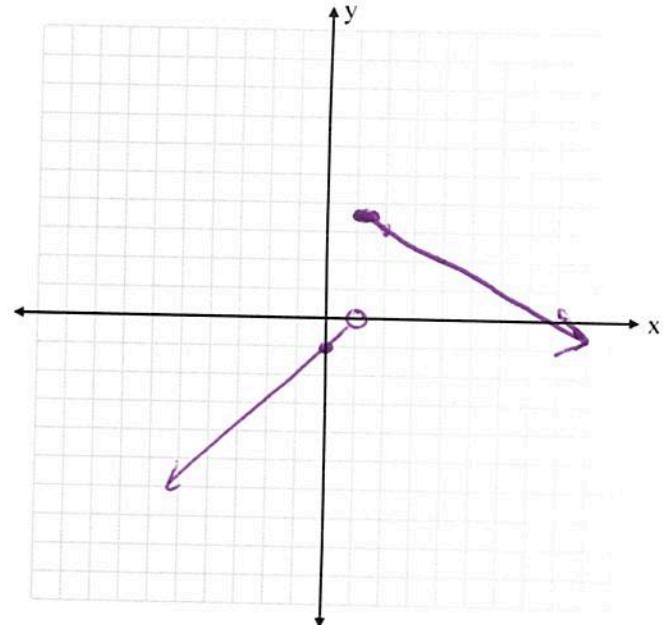


Instructions: Show all work. Use exact answers unless otherwise asked to round.

1. Sketch the graph of the function $f(x) = \begin{cases} x - 1, & x < 1 \\ -\frac{1}{2}x + 4, & x \geq 1 \end{cases}$



2. For the function above, find the following:

- a. Any symmetry of the function.

None

- b. The intervals on which the graph is increasing, decreasing or constant.

increasing $(-\infty; 1)$ decreasing $(1, \infty)$

- c. Any relative maxima or minima.

max at $(1, \frac{7}{2})$ no min

- d. The domain and range.

D: $(-\infty, \infty)$ all reals

R: $\{-\infty, \frac{7}{2}\}$

3. Consider the function $f(x) = x^2 + 6x + 1$. Find $f(x+1)$.

$$\begin{aligned} f(x+1) &= (x+1)^2 + 6(x+1) + 1 = \\ &= x^2 + 2x + 1 + 6x + 6 + 1 = \\ &= x^2 + 8x + 8 \end{aligned}$$

4. State the domain and range of the following functions. Write your answers in interval notation.

a. $f(x) = \frac{x}{2x-3}$

$$\begin{aligned}2x-3 &= 0 \\2x &= 3 \\x &= \frac{3}{2}\end{aligned}$$

$$D: (-\infty, \frac{3}{2}) \cup (\frac{3}{2}, \infty)$$

$$x \neq \frac{3}{2}$$

$$R: (-\infty, \frac{1}{2}) \cup (\frac{1}{2}, \infty)$$

$$y = \frac{1}{2}$$

HA

b. $g(x) = \sqrt{4x+7} + 1$

$$D: [\frac{7}{4}, \infty)$$

$$R: [1, \infty)$$

$$4x+7 \geq 0$$

$$4x \geq -7$$

$$x \geq -\frac{7}{4}$$

5. Consider the functions $f(x) = 4x - 1$ and $g(x) = x^2 + 3$. Find the following:

a. $(f+g)(3)$

$$(f+g)(x) = 4x - 1 + x^2 + 3 = x^2 + 4x + 2 \quad (f+g)(3) = 3^2 + 4(3) + 2 = 9 + 12 + 2 = 23$$

b. $(fg)(x)$

$$(4x-1)(x^2+3) = 4x^3 + 12x - x^2 - 3 = 4x^3 - x^2 + 12x - 3$$

c. $\left(\frac{g}{f}\right)(x)$

$$\frac{x^2+3}{4x-1}$$

6. Find and simplify the difference quotient for $f(x) = 4x^2 - 7x + 5$. Recall the difference quotient is $\frac{f(x+h)-f(x)}{h}$.

$$\frac{4(x+h)^2 - 7(x+h) + 5 - (4x^2 - 7x + 5)}{h} =$$

$$\frac{4x^2 + 8xh + 4h^2 - 7x - 7h + 8 - 4x^2 + 7x - 5}{h} =$$

$$\frac{8xh + 4h^2 - 7h}{h} = \frac{h(8x + 4h - 7)}{h} =$$

$$8x + 4h - 7$$

$$\begin{aligned}(x+h)^2 &= \\x^2 + 2xh + h^2 &\end{aligned}$$