

**Instructions:** Show all work. Answer each question as completely as possible. Use exact values. For counting problems you may use scientific notation (with three significant figures) for any numbers larger than a million.

1. Count the following election.

Rank/# of Votes	150	130	120	100
1 <sup>st</sup>	C	D	B	A
2 <sup>nd</sup>	D	A	C	C
3 <sup>rd</sup>	A	B	A	B
4 <sup>th</sup>	B	C	D	D

a. Use the plurality method with elimination to determine the winner.

$$\begin{array}{l} \cancel{A=150} \quad \cancel{B=120} \quad C=150 \quad D=130 \\ \quad \quad \quad \quad \quad 250 \\ \quad \quad \quad \quad \quad 370 \end{array}$$

C wins

b. Use the information obtained from part (a) to extend the rankings to 2<sup>nd</sup>, 3<sup>rd</sup>, and 4<sup>th</sup> place.

$$\begin{array}{l} C = 1^{\text{st}} \\ D = 2^{\text{nd}} \\ B = 3^{\text{rd}} \\ A = 4^{\text{th}} \end{array}$$

c. Compare the winner of this plurality with elimination method with the plurality method. Is this an independence of irrelevant alternatives violation? Why or why not?

C wins plurality method.

Since losing candidates dropping out of the race did not change the winner, this is not an IIA violation.

2. Consider an election that resulted in the following preference table.

Place/# of Votes	7	6	5	3
1 <sup>st</sup>	A	B	C	D
2 <sup>nd</sup>	B	A	B	C
3 <sup>rd</sup>	C	C	A	B
4 <sup>th</sup>	D	D	D	A

a. Determine the winner of the election using the plurality with elimination method.

$A = 7$      $B = 6$      $C = 5$      $D = 3$   
           13                   8  
 A wins

b. But supporters of D find out of the results, and decide to change their votes from D to A as shown in the table below. Recount the election.

Place/# of Votes	7	6	5	3
1 <sup>st</sup>	A	B	C	A
2 <sup>nd</sup>	B	A	B	D
3 <sup>rd</sup>	C	C	A	C
4 <sup>th</sup>	D	D	D	B

$A = 10$      $B = 6$      $C = 5$      $D = 0$   
                   11

B wins

c. Is this a violation of a fairness criterion? Which one? Why or why not?

This is a violation of the monotonicity criterion.  
 A won the first round, gained more first place votes in round 2, but lost the election anyway.