

Instructions: Show all work. Answer each question as completely as possible. Use exact values. For counting problems you may use scientific notation (with three significant figures) for any numbers larger than a million.

1. Count the following election.

Rank/# of Votes	150	130	120	100
1 st	C	D	B	A
2 nd	D	A	C	C
3 rd	A	B	A	B
4 th	B	C	D	D

a. Use the plurality method to count the votes.

C wins since C has the most first-place votes.

b. Use the method of pairwise comparisons to count the vote.

A-B	150 + 130 + 100	vs. 120	A
A-C	130 + 100	vs. 150 + 120	C
A-D	120 + 100	vs. 150 + 130	D
B-C	130 + 120	vs. 150 + 100	tie
B-D	120 + 100	vs. 150 + 130	D
C-D	150 + 100 + 120	vs. 130	C

$$\begin{aligned}
 A - 1 &= 1 \\
 B - \frac{1}{2} &= \frac{1}{2} \\
 C - 1\frac{1}{2} &= 2\frac{1}{2} \\
 D - 11 &= 2
 \end{aligned}$$

C wins

c. Use the Borda Count method to count the votes.

$$\begin{aligned}
 A &= 2(150) + 3(130) + 2(120) + 4(100) = 1330 \\
 B &= 1(150) + 2(130) + 4(120) + 2(100) = 1090 \\
 C &= 4(150) + 1(130) + 3(120) + 3(100) = 1390 \leftarrow C \text{ wins} \\
 D &= 3(150) + 4(130) + 1(120) + 1(100) = 1190
 \end{aligned}$$

d. Is the winner the same in each case?

Yes