

Instructions: Use permutations to count the number of things in each scenario. Write the permutation notation, express in terms of factorials, reduce, and then use the calculator if needed.

1. Suppose you and five more friends are standing in line. In how many different orders can you and your friends stand in line?

$$6P6 = 6! = 720$$

2. A deck of cards has 52 cards in it. You draw 5. In how many ways can the order of those 5 cards come out?

$$52P5 = 311,875,200$$

3. Suppose a lottery drawing has 39 balls in the machine. 7 balls are chosen. How many different ways can those 7 balls come out of the machine?

$$39P7 = 7.75 \times 10^{10}$$

4. How many different ways can you organize the numbers 1, 2, 3, and 4? Once you find how many, list them all.

$$4P4 = 4! = 24$$

| | | | | | |
|------|------|------|------|------|------|
| 1234 | 1243 | 1324 | 1342 | 1423 | 1432 |
| 2134 | 2143 | 2314 | 2341 | 2413 | 2431 |
| 3124 | 3142 | 3214 | 3241 | 3412 | 3421 |
| 4123 | 4132 | 4213 | 4231 | 4312 | 4321 |

5. There are 16 balls in billiard. In how many different orders can the balls be dropped in pockets if they all have to be cleared from the table?

$$16P16 = 16! = 2.09 \times 10^{13}$$

6. If a math department has 17 faculty members available to serve as officers for an advisory committee, in how many different ways can the officers be chosen?

if there are 4 officers (President, Vice President, Secretary & Treasurer) Then ${}_{17}P_4 = 57,120$

7. Suppose you choose an 8 digit password that allows letters of both cases and numbers. How many different possibilities are there if you don't reuse any letter twice?

$$52 (= 26+26+10)$$

$${}_{52}P_8 = 1.36 \times 10^{14}$$

8. How many different ways can we organize the letters A, B, C, D, E? Can you list them all?

$${}_5P_5 = 5! = 120$$

| | | | | | |
|-------|-------|-------|-------|-------|-------|
| ABCDE | ABCED | ABDEC | ABDCE | ACBDE | ACBDE |
| ACDBE | ACDEB | ADBCE | ADBEC | ADCBE | ADCEB |
| ADEBC | ADECB | ABECD | ABEDC | AEBDC | AEBDC |
| AECBD | AECDB | AEDBC | AEDCB | BACDE | BACED |
| BADCE | BADEC | BAECD | BAEDC | BCADE | BCAED |
| BCDAE | BCDEA | BCEAD | BCEDA | BDACE | BDAEC |
| BDCAE | BDCEA | BEACD | BEADC | BECAD | BECDA |
| BEDAC | BEDCA | ACEBD | ACEDB | BDEAC | BDECA |
| CABDE | CABED | CADBE | CADEB | CAEBD | CAEDB |
| CBADE | CBAED | CBDAE | CBDEA | CBEAD | CBEDA |
| CDABE | CDAEB | CDBAE | CDBEA | CDEAB | CDEBA |
| CEABD | CEADB | CEBAD | CEBDA | CEDBA | CEDAB |
| DABCE | DABEC | DACBE | DACEB | DAEBC | DAECB |
| DBACE | DBACE | DBCAE | DBCEA | DBEAC | DBECA |
| DCABE | DCAEB | DCBAE | DCBEA | DCEAB | DCEBA |
| DEABC | DEACB | DEBAC | DEBCA | DECAB | DECBA |
| EABCD | EABDC | EACBD | EACDB | EADBC | EADCB |
| EBACD | EBADC | EBCAD | EBCDA | EBDAC | EBDCA |
| ECABD | ECADB | ECBDA | ECBAD | ECDAB | ECDBA |
| EDABC | EDACB | EDBAC | EDBCA | EDCAB | EDCBA |